

## POLARIMETRIC OBSERVATIONS OF $\sigma$ ORIONIS E

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### ABSTRACT

Some massive stars possess strong magnetic fields that confine plasma in the circumstellar environment. These *magnetospheres* have been studied spectroscopically, photometrically, and, more recently, interferometrically. Here we report on the first firm detection of a magnetosphere in continuum linear polarization, as a result of monitoring  $\sigma$  Ori E at the Pico dos Dias Observatory. The non-zero intrinsic polarization indicates an asymmetric structure whose minor elongation axis is oriented  $150^\circ 0'$  east of the celestial north. A modulation of the polarization was observed with a period of half of the rotation period, which supports the theoretical prediction of the presence of two diametrically opposed, corotating blobs of gas. A phase lag of  $-0.085$  was detected between the polarization minimum and the primary minimum of the light curve, suggestive of a complex shape of the plasma clouds. We present a preliminary analysis of the data with the Rigidly Rotating Magnetosphere model, which could not reproduce simultaneously the photometric and polarimetric data. A toy model comprising two spherical corotating blobs joined by a thin disk proved more successful in reproducing the polarization modulation. With this model we were able to determine that the total scattering mass of the thin disk is similar to the mass of the blobs ( $2M_b/M_d = 1.2$ ) and that the blobs are rotating counterclockwise on the plane of the sky. This result shows that polarimetry can provide a diagnostic of the geometry of clouds, which will serve as an important constraint for improving the Rigidly Rotating Magnetosphere model.

*Key words:* circumstellar matter – polarization – stars: individual ( $\sigma$  Ori E) – stars: magnetic field

*Online-only material:* color figures

### 1. INTRODUCTION

The helium-strong star  $\sigma$  Orionis E (HD 37479; B2 Vpe;  $m_V = 6.66$ ) has long been known to possess a circumstellar magnetosphere that is formed by wind plasma that is trapped by a strong dipolar magnetic field ( $\approx 10$  kG; Landstreet & Borra 1978). The presence of this magnetosphere can be inferred by the eclipse-like dimmings on its light curve, which is thought to occur when plasma clouds go in front of the star twice every rotation cycle (Townsend et al. 2005; Hesser et al. 1977; Groote & Hunger 1982). This star has been the testbed for important advancements in our theoretical understanding of these magnetospheres. The Rigidly Rotating Magnetosphere (RRM) models of this star were successful in reproducing the observed variability in emission line profiles and photometry (Townsend et al. 2005).

Polarization is a very useful technique that allows one to probe the geometry of the circumstellar scattering material without angularly resolving it (e.g., Brown & McLean 1977). Kemp & Herman (1977) carried out the first polarimetric observations of the  $\sigma$  Ori system, but their results were largely inconclusive because of the small values of the intrinsic polarization. In this Letter we present the results of high-precision ( $\sigma \sim 0.01\%$ ) polarization monitoring of  $\sigma$  Ori E, which has resulted in the first firm detection of the polarization modulation produced by a corotating magnetosphere.

### 2. OBSERVATIONS

Broadband linear polarization data were obtained from 2010 August to 2011 September, using the IAGPOL image polarimeter attached to the 0.6 m Boller and Chivens telescope at Pico dos Dias Observatory (OPD/LNA). We used a CCD camera with a

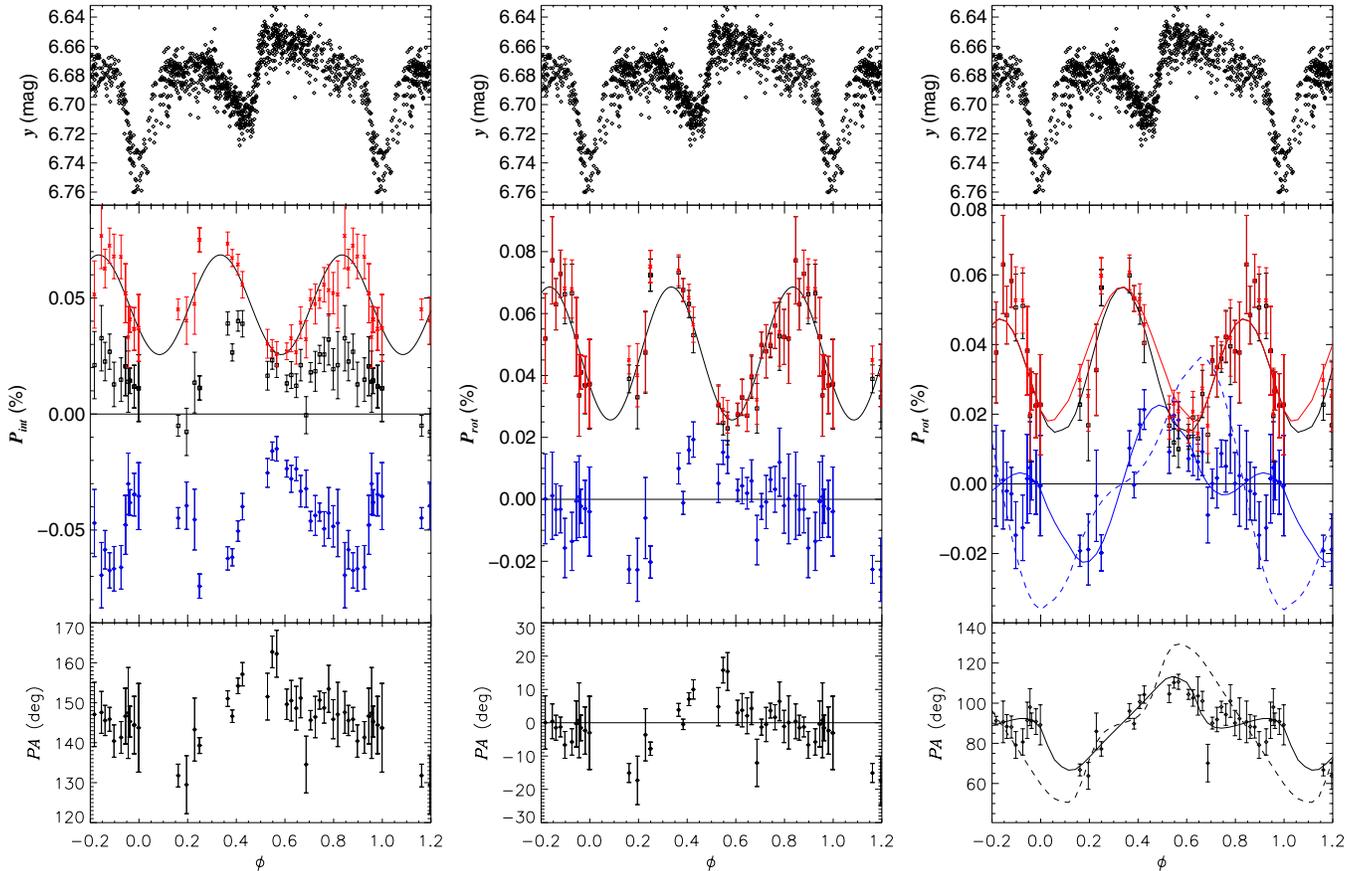
polarimetric module described in Magalhães et al. (1996), consisting of a rotating half-wave plate and a calcite prism placed in the telescope beam. In each observing run at least one polarized standard star was observed in order to calibrate the observed position angle. HD 23512 and HD 187929 were used as polarized standards.

Although typical polarimetric observations consists of eight consecutive wave plate positions (hereafter WPP) separated by  $22.5^\circ$  (Carciofi et al. 2007), in this work we chose to use 16 consecutive WPPs in order to increase the signal-to-noise ratio. Also, to reach the high accuracy needed to monitor the modulation of the polarization, a large number of frames (typically from 20 to 100) were obtained at each WPP. Since the exposure times ranged from 0.3 to 1 s per frame, the temporal resolution of our observations varies from 7 to 34 minutes, including telescope and instrument overheads. These values are short enough to temporally resolve the polarimetric variation over the 1.19-day period of the star. Details of the data reduction can be found in Magalhães et al. (1984).

### 3. INTERSTELLAR POLARIZATION

Kemp & Herman (1977) report similar values of the polarization for  $\sigma$  Ori AB,  $\sigma$  Ori C, and  $\sigma$  Ori D, which suggests that all these stars belong to the same physical system, and that the measured polarization is of interstellar (IS) origin.

We measured the *BVRI* polarization of  $\sigma$  Ori AB and C and our results are largely consistent with the ones of Kemp & Herman (1977). We used our measured *V*-band polarization of  $\sigma$  Ori AB ( $P = 0.351(15)\%$ ;  $86^\circ 7'$ ;  $Q = -0.348(15)\%$ ;  $U = 0.040(15)\%$ ) as an estimate of the IS polarization toward  $\sigma$  Ori E.



**Figure 1.** Variation of the intrinsic polarization of  $\sigma$  Ori E compared with photometric variations in the  $y$  filter. Top panels:  $y$  filter photometric data from Hesser et al. (1977), folded in phase. Middle panels: intrinsic  $P$  (red),  $Q$  (black), and  $U$  (blue). Bottom panels: intrinsic position angle. Left plot: the polarization data are displayed in the equatorial reference frame. The polarization of  $\sigma$  Ori AB was used as a measure of the IS polarization. Middle plot: same as the left plot, rotated such that  $\langle U_{\text{int}} \rangle = 0$ . Right plot: polarization compared to the single-scattering model. The solid line is for our best-fitting model with  $i = 70^\circ$  and the dashed line is for  $i = 110^\circ$ . For this plot we used the estimate for the IS polarization and  $\theta$  made in Section 6.

(A color version of this figure is available in the online journal.)

#### 4. RESULTS

The  $V$ -band  $\sigma$  Ori E observations are shown in the left plot of Figure 1. The data were folded in phase ( $\phi$ ) using the ephemerides of Townsend et al. (2010). Shown is the intrinsic polarization, calculated by subtracting the IS polarization, estimated using  $\sigma$  Ori AB, from the observed  $Q$  and  $U$  Stokes parameters. The polarization has a double-peaked structure, with maxima of about 0.07% occurring at phases around 0.3 and 0.8 and minima occurring around phases 0.1 and 0.6. We note that the values reported here are in broad agreement with the data of Kemp & Herman (1977), but a more quantitative comparison is hampered by the insufficient accuracy of the latter data.

There is a clear anti-correlation between the photometric and polarimetric variations, with the polarization minima roughly coinciding with the photometric maxima and vice versa, but there are important differences between the two curves. One such difference lies in their symmetry: the photometry is clearly asymmetric, with the secondary minimum occurring at about phase 0.4 (the primary minimum occurs at  $\phi = 0$  by definition), and the behavior of the two inter-minima being very different from each other. The polarization curve, however, seems to be roughly symmetric with respect to  $\phi \approx 0.6$ . That the asymmetry is seen in the photometry but not in the polarization is further supporting evidence that—as hypothesized in Townsend et al. (2005)—the asymmetric light

curve arises due to contamination of the circumstellar signal by a photospheric signal. That is, the photometric variations come from a combination of magnetospheric eclipses and photospheric abundance inhomogeneities, and therefore lack rotational symmetry; but conversely, because the polarization variations come solely from magnetospheric electron scattering, we do see rotational symmetry in their case.

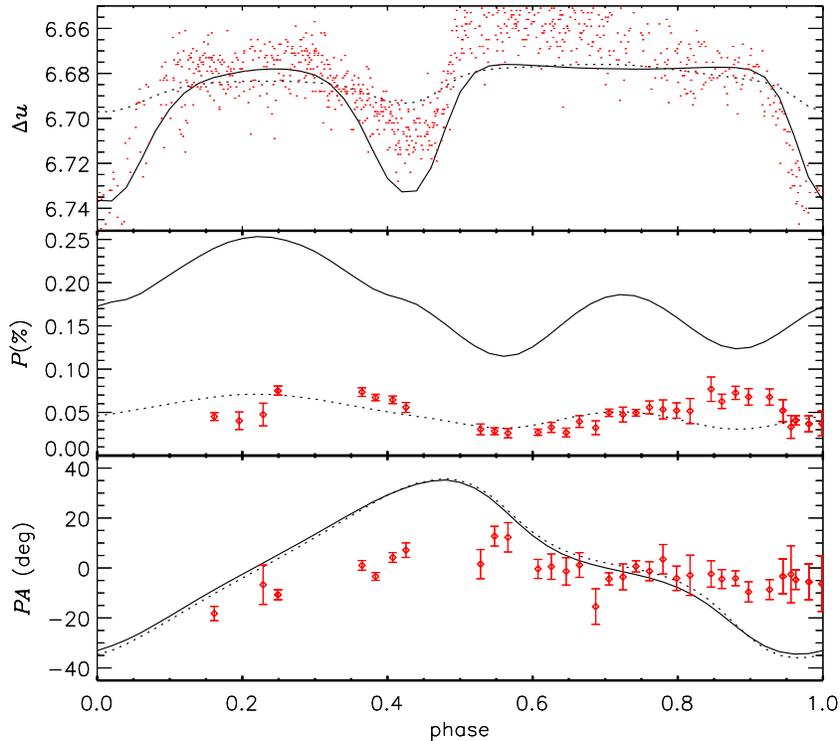
In order to determine the location of the polarization minimum, we fitted the data between  $\phi = 0.45$  and 0.75 with a parabola, using the Levenberg–Marquardt algorithm (Marquardt 1963). We find that the minimum of the intrinsic polarization occurs at  $\phi_{\text{min}} = 0.61 \pm 0.03$ . To determine the location of the maximum, the same procedure was applied to the data between  $\phi = 0.7$  and 1. According to this fit the maximum of the polarization occurs at  $\phi_{\text{max}} = 0.84 \pm 0.04$ .

To further assess the symmetry of the data, we fitted the polarization data with the following function:

$$P(\phi) = P_0 + A \cos[4\pi(\phi - \delta)], \quad (1)$$

which implicitly assumes a period of half of the orbital period for the polarimetric data. The result of the fit gives  $P_0 = 0.0471\% \pm 0.0009\%$ ,  $A = 0.021\% \pm 0.001\%$ , and  $\delta = -0.17 \pm 0.01$ , with a reduced  $\chi^2 = 0.67$ . The fitted function is displayed as the black line in the middle plot of Figure 1.

The data seem to be well represented by Equation (1), which indicates that, contrary to the photometry, the polarization curve



**Figure 2.** Modeling of the intrinsic polarization of  $\sigma$  Ori E using the RRM model (observations are in red). The only free parameter is the maximum number density in the magnetosphere, which was set to  $10^{12} \text{ cm}^{-3}$  (solid lines) to reproduce the depth of the eclipses and  $2.5 \times 10^{11} \text{ cm}^{-3}$  (dotted lines) to reproduce the amplitude of the linear polarization.

(A color version of this figure is available in the online journal.)

is roughly symmetric. From Equation (1), the positions of the minima are  $\phi = 0.08$  and  $0.58$ , and the maxima are at  $\phi = 0.33$  and  $0.83$ . Those values are in good agreement with the phases derived above via a parabola fitting. The minimum and maximum values of the polarization are, respectively,  $P_0 - A = 0.026\% \pm 0.001\%$  and  $P_0 + A = 0.068\% \pm 0.001\%$ .

An important feature of the intrinsic polarization of  $\sigma$  Ori E is that it is never zero. This indicates that there is some degree of asymmetry of the scattering material (as seen projected onto the plane of the sky) throughout the entire rotation period.

The data shown in the left plot of Figure 1 are in the equatorial frame. The weighted average of all the data gives a value of  $\langle Q_{\text{int}} \rangle = 0.023\%$  and  $\langle U_{\text{int}} \rangle = -0.040\%$ , which, in turn, results in an average position angle of  $\langle \theta_{\text{int}} \rangle = 150^\circ.0$ . This value tells us the (average) direction of the minor axis of the asymmetric structure. Furthermore, the small variation of the position angle (Figure 1, left) tells us that the direction of the minimum elongation axis changes little ( $\approx 10^\circ$ – $15^\circ$ , at most) as the star rotates.

This last point is better understood if we rotate the intrinsic polarization by  $\langle \theta_{\text{int}} \rangle$  so that the average value of  $U$  is zero (Figure 1, right plot). In this new frame, we see that the amplitude of the rotational modulation of  $U$  is small. If we assume that the symmetry axis is parallel to the rotation axis, we conclude that the projected axis of symmetry of the magnetosphere varies little as the star rotates. As discussed below, this has quite important consequences for the RRM model.

Another noteworthy feature of the polarization curve is that there is a phase shift of  $-0.085$  between the primary minimum of the light curve and the polarization minimum. The RRM model of Townsend et al. (2005) predicts the existence of two plasma clouds corotating with the star. If the clouds were symmetrical and the photospheric fluxes were homogeneous,

there should be no phase difference between the polarization and photometric curves; the observed phase shift, therefore, is likely a result of cloud asymmetries and photospheric abundance inhomogeneities.

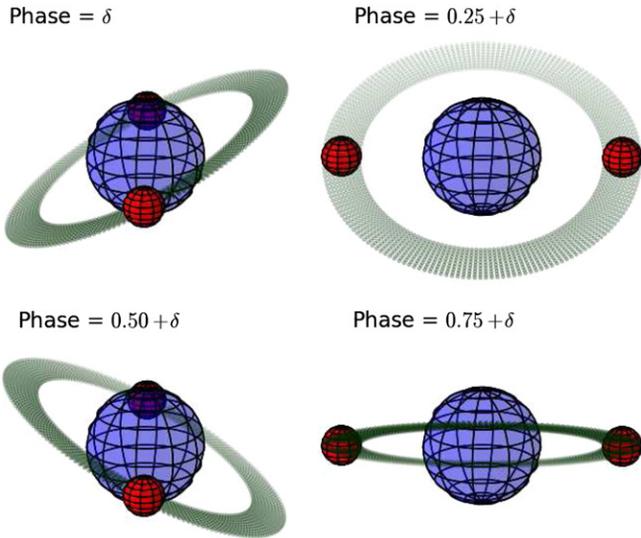
## 5. RRM MODEL

Townsend et al. (2005) applied the RRM model to  $\sigma$  Ori E with good success. This model predicts the accumulation of circumstellar plasma in two corotating clouds, situated in magnetohydrostatic equilibrium at the intersections between the magnetic and rotational equators. Comparison with the available data (photometry and  $H\alpha$  line profiles) showed that the model provided a good quantitative description of the circumstellar environment.

In an attempt to reproduce the observed polarization modulation of  $\sigma$  Ori E, we fed the predicted density distribution of the RRM model of Townsend et al. (2005) to the HDUST radiative transfer code (Carciofi & Bjorkman 2006). Since all stellar and geometrical parameters were taken from Townsend et al. (2005), the only free parameter in the model is the density scale of the magnetosphere.

The results of this modeling are shown in Figure 2. We could not find a model that simultaneously matched both the photometry and the polarimetry. A higher density model (solid line) that matches the depth of the photometric eclipses predicts a polarization amplitude that is three times larger than what is observed. Conversely, a lower density model that reproduces the amplitude of the polarization fails to reproduce the photometric amplitude.

Furthermore, the detailed shape of the polarization curve, in particular the position angle variation, is not well matched. Since the polarization position angle is sensitive to the geometry of the scattering material, this discrepancy indicates that the primary



**Figure 3.** Geometric conception of the “dumbbell + disk” model to scale.  
(A color version of this figure is available in the online journal.)

difficulty with the basic RMM model is the shape of its density distribution.

## 6. SINGLE-SCATTERING MODEL

We now explore what changes must be made to the basic RRM model to better reproduce the shape of the polarimetric variability. The RRM predicts the existence of diametrically opposed plasma clouds confined in the rotational equator and a diffuse plasma disk close to the magnetic equator. Based on this idea, we developed a simple toy model for  $\sigma$  Ori E that consists of two elements: (1) a thin uniform disk tilted by an angle  $\psi$  from the rotational equator and (2) a pair of spherical blobs situated in the equatorial plane at the intersection between this plane and the magnetic equator, thus forming a “dumbbell-like” structure. This configuration is illustrated in Figure 3, for several orbital phases and for a viewing angle of  $70^\circ$ .

Since the polarization is small, we may perform the calculation of the  $Q$  and  $U$  Stokes parameters as a function of orbital phase for a given inclination angle  $i$  following a simple single-scattering approach (valid only in the optically thin limit). The scattered flux is first determined in the frame of the star using the formalism described in Bjorkman & Bjorkman (1994, Equation (6)) and then rotated to the frame of the observer (Bjorkman & Bjorkman 1994, Equation (20)).

For this initial study, we adopted five fixed parameters, listed in Table 1, whose values were based on the models of Townsend et al. (2005). They are the stellar radius,  $R_*$ , the distance of the blobs from the star,  $d_b$ , the size of the blobs,  $R_b$ , the geometrical thickness of the disk,  $H_d$ , and the inclination angle,  $i$ . The adopted value for  $R_{\text{blob}}$  is somewhat arbitrary, since in the limit of  $R_{\text{blob}} \ll R_*$  and in the single-scattering approximation, a large, tenuous blob is roughly equivalent to a dense, small blob. For the same reason, the disk geometrical thickness is also somewhat arbitrary: if the single-scattering approximation holds, a thinner, denser disk is equivalent to a thicker, less dense disk. In other words, what really controls the polarization level of each component is their total scattering mass. For the inclination angle we adopt two possible values:  $i = 70^\circ$ , corresponding to a projected counterclockwise rotation of the blobs on the sky and  $180^\circ - 70^\circ = 110^\circ$ , corresponding to a clockwise rotation.

**Table 1**  
Parameters of the Single-scattering Model

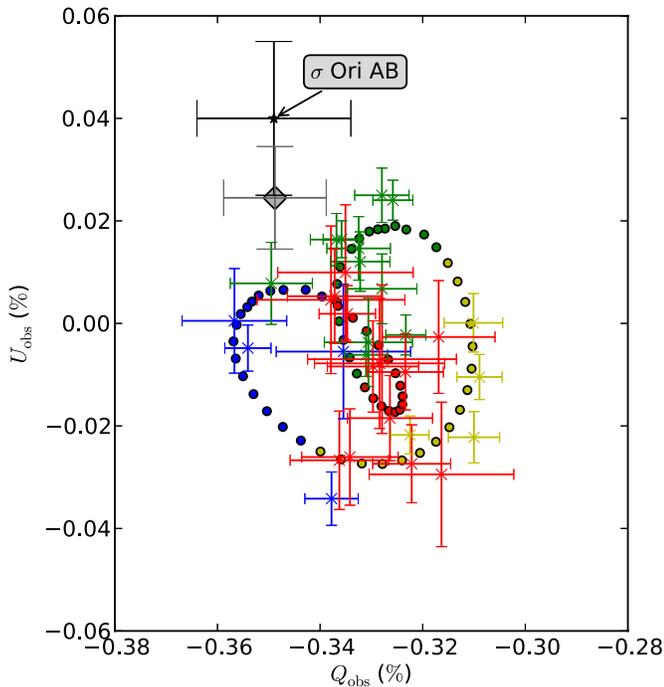
Parameter	Value	Type
$i$ (deg)	70 or 110	Fixed
$R_*$ ( $R_\odot$ )	4.3	Fixed
$d_b$ ( $R_*$ )	2.4	Fixed
$R_b$ ( $R_*$ )	1/3	Fixed
$H_d$ ( $R_*$ )	0.01	Fixed
$n_e^b$ ( $e^- \text{ cm}^{-3}$ )	$1.0^{+0.6}_{-0.9} \times 10^{12}$	Fitted
$n_e^d$ ( $e^- \text{ cm}^{-3}$ )	$2.7 \pm 1 \times 10^{12}$	Fitted
$\psi$ (deg)	28	Fitted
$Q_{\text{IS}}$ (%)	$-0.35 \pm 0.01$	Fitted
$U_{\text{IS}}$ (%)	$0.025 \pm 0.010$	Fitted
$\theta$ (deg)	$150 \pm 7$	Fitted
$\delta$	$-0.17 \pm 0.02$	Fitted

In this analysis we made *no previous assumptions about the IS polarization*, i.e., we fitted directly the observed  $Q$  and  $U$  Stokes parameters. The adopted modeling procedure is as follows.

1. Choose values for electron number density in the blob and disk ( $n_e^b$  and  $n_e^d$ ), the phase lag,  $\delta$ , between the photometric primary minimum ( $\phi = 0$ ) and the orbital phase where the blobs are aligned with the line of sight, the tilt angle of the disk,  $\psi$ , and the position angle of the equatorial plane in the plane of the sky,  $\theta$ . These five parameters define a unique model for the intrinsic  $Q$  and  $U$  in the equatorial frame.
2. Choose values for  $Q_{\text{IS}}$  and  $U_{\text{IS}}$  and use them to calculate synthetic observed  $Q$  and  $U$  parameters.
3. Calculate the reduced  $\chi^2$  of the model.
4. Repeat steps 1 and 3 for several hundred of values for the seven free parameters and choose the model with minimum  $\chi^2$ .

The parameters of our best-fitting model (reduced  $\chi^2 = 2.8$ ) are listed in Table 1. The estimated errors are for a 95% confidence interval. A notable result is that the IS polarization, independently obtained by this analysis, is consistent (within the errors) with the estimate made using  $\sigma$  Ori AB as a measure of the IS. Both the orientation of the equatorial plane in the sky ( $\theta$ ) and the phase lag ( $\delta$ ) are consistent with the estimate made in Section 4. The resulting blob density corresponds to an electron optical depth of  $\tau = 0.13$ , which does not violate the optically thin assumption. It is worth mentioning that our estimate for the electron density in the blobs,  $10^{12} e^- \text{ cm}^{-3}$ , is in good agreement with the values derived by Groote & Hunger (1982) and Smith & Bohlender (2007) using the Inglis–Teller formula. From the best-fitting parameters one can calculate the mass of each model component. Assuming a molecular weight of 0.6, which corresponds to a fully ionized gas with solar chemical composition, the mass of each blob is  $M_b = 6.0 \times 10^{-12} M_\odot$  and the mass of the disk is  $M_d = 1.0 \times 10^{-11} M_\odot$ . Therefore, we obtain that both components have similar masses ( $2M_b/M_d = 1.2$ ).

In Figure 1 (right plot), we show the observations corrected by the IS polarization of Table 1. The solid curves correspond to the best-fitting single-scattering model. The two minima of the model polarization occur at the phases for which the two blobs are aligned with the line of sight. At these phases, the model  $Q$  parameter is the minimum and the  $U$  parameter is the maximum (negative for  $\phi \approx \delta$  and positive for  $\phi \approx 0.5 + \delta$ ), because the disk dominates the polarized flux at these phases. Conversely, the polarized flux is dominated by the blobs at the phases at



**Figure 4.**  $QU$  plot of the observed data (points with error bars). The orbital phase correspondence of the points is as follows: blue,  $\delta - (\delta + 0.25)$ , orange,  $(\delta + 0.25) - (\delta + 0.50)$ , green,  $(\delta + 0.50) - (\delta + 0.75)$ , and red,  $(\delta + 0.75) - \delta$ . The filled circles show the best-fitting model of Table 1. The IS polarization of  $\sigma$  Ori AB is indicated. The gray diamond shows the IS of Table 1.

which the blobs are on the side of the star ( $\phi \approx 0.25 + \delta$  and positive for  $\phi \approx 0.75 + \delta$ ).

An interesting result is that the data allowed us to firmly establish that the blobs are rotating counterclockwise on the plane of the sky. In the right plot of Figure 1, the solid curves show the best-fitting model for  $i = 70^\circ$  (reduced  $\chi^2 = 2.8$ ) while the dotted curves correspond to the best-fitting model with  $i = 110^\circ$  (reduced  $\chi^2 = 5.1$ ). The former is clearly a much better fit to the data.

An alternative comparison between the data and the single-scattering model is made in Figure 4, where we plot the observed (i.e., uncorrected for IS polarization)  $U$  versus  $Q$  parameters. The blue points correspond to the phase range  $\delta - (\delta + 0.25)$ , the orange ones from  $(\delta + 0.25) - (\delta + 0.50)$ , the green ones from  $(\delta + 0.50) - (\delta + 0.75)$ , and the red ones from  $(\delta + 0.75) - \delta$ . In the  $QU$  plane the behavior of the data is quite different from the first half-cycle to the second: while in the first half (blue and orange points) the data forms a nearly circular outer loop, in the second half (green and red points) there is an inward incursion. The model reproduces this behavior.

It is important to point out that the two-component model (blob+disk) adopted by us is required to produce such a behavior in the  $QU$  plane. For instance, a model with only the blobs would form a symmetric double ellipse in the  $QU$  plane, while a model with only the tilted disk would result in a shape resembling a crescent moon. The observed curve, composed of an outer loop and an inner incursion, can only be obtained by a combination of these two components.

## 7. CONCLUSIONS

The polarimetric data presented here for  $\sigma$  Ori E have an accuracy of at least one order magnitude better than those shown in the work of Kemp & Herman (1977) and thus represent

the first firm detection of the polarization modulation of a corotating magnetosphere. The intrinsic polarization, calculated using  $\sigma$  Ori AB as a measure of the IS polarization, displays a roughly symmetric sinusoidal curve ranging from 0.02% to 0.08%, with a period of half of the orbital period and a phase lag of  $-0.085$  between the polarization minimum and the primary minimum of the light curve. The polarization position angle is also variable. Its mean value of  $150^\circ 0$  indicates that the minor elongation axis of the asymmetric structure around  $\sigma$  Ori E is oriented  $150^\circ 0$  east of the celestial north.

A preliminary analysis made with the RRM model (Townsend et al. 2005) suggests that it is difficult to fit both the photometry and the polarization simultaneously. This seems to imply that the geometry of the plasma clouds, as predicted by the current version of the model, is incorrect.

However, the data were well reproduced by a two-component model, consisting of two spherical, diametrically opposed blobs and a disk tilted with respect to the rotational equator. This model was physically motivated by the RRM model, which predicts accumulation of centrifugally supported wind plasma in a disk-like structure with the highest densities (corresponding to the blobs) at the points where the magnetic equator intersects the rotational equator. This model provided useful constraints on the total scattering mass of each component. Also, it provided an independent estimate for the IS polarization, as well as for the orientation of the equatorial direction in the plane of the sky. Our best-fitting model suggests that the mass of each blob is  $M_b = 0.6 \times 10^{-12} M_\odot$  and the mass of the disk is  $M_d = 1.0 \times 10^{-11} M_\odot$ , which indicates that both components have similar masses ( $2M_b/M_d = 1.2$ ). Also, the tilt angle of the disk with respect to the plane of the sky is  $28^\circ$ , similar to the angle between the rotational and magnetic axes (Townsend et al. 2005). Finally, the model allowed us to determine that the blobs are rotating counterclockwise on the plane of the sky.

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